

Adaptive massive MIMO for fast moving connected vehicles: **It will work with Predictor Antennas!**

ITG INFORMATION TECHNOLOGY SOCIETY
IN THE VDE

22nd International 
WSA 2018
ITG Workshop on Smart Antennas
March 14 - 16 2018, Bochum, Germany



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- II. Measurement Setup
- III. Performance Evaluation Methodology
- IV. Results
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I. Motivation

The Problem of Channel Aging

The **increased spectral efficiency of massive MIMO** can reduce the cost of wireless access.

The massive MIMO **performance crucially relies on Channel State Information** at transmitter (CSIT) side.

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- Delay τ at the network side (e.g. CSI feedback delay in FDD, low channel training rates in TDD, processing delays at the base station)

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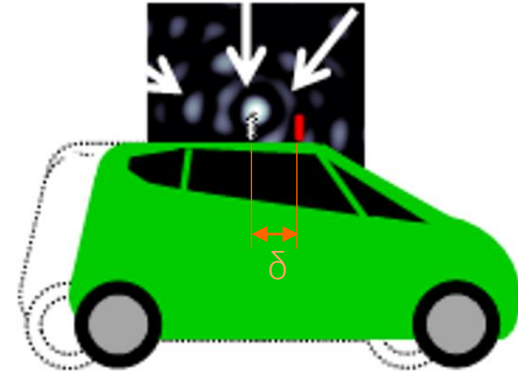
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Channel Training in UL at time t_0



Data Transmission in DL at time $t_0 + \tau$



The Impact of Channel Aging – A Quantitative Example

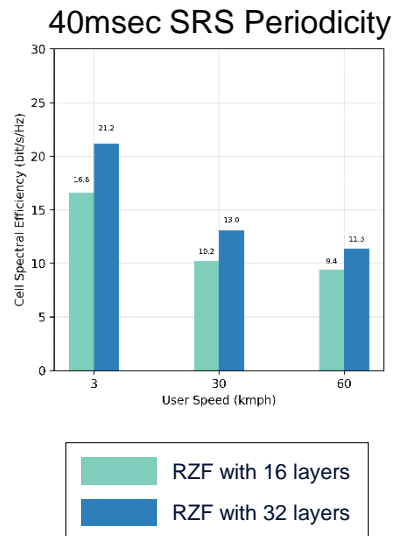
System-level Simulations

- 3GPP 38.901 Urban Micro TDD scenario,
- 57 cells, 200m ISD, on average 20 users per cell,
- 64 TXRUs, 41dBm Tx Pwr @10MHz BW, $f_c=3.5\text{GHz}$,
- Full-buffer users (best effort traffic) with x-pol. antennas (2 layers/user),
- SRS-based channel estimation in UL,
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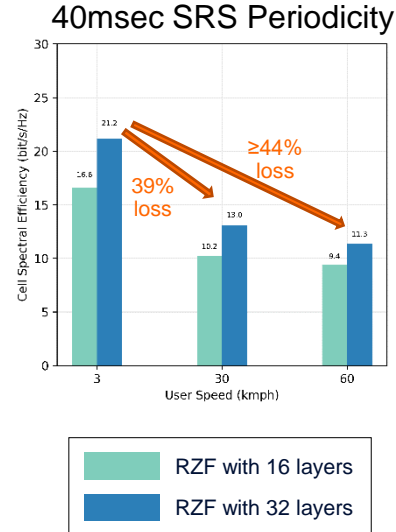
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Significant performance losses (>43% @ 60kmph) due to channel aging

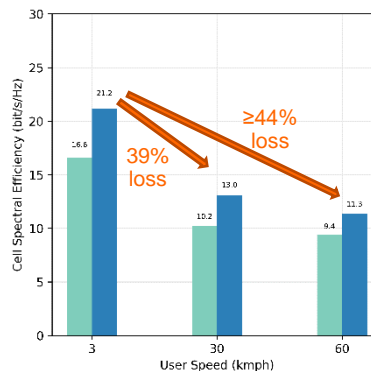
→ Channel prediction methods will help to maintain the massive MIMO gains at higher user speeds

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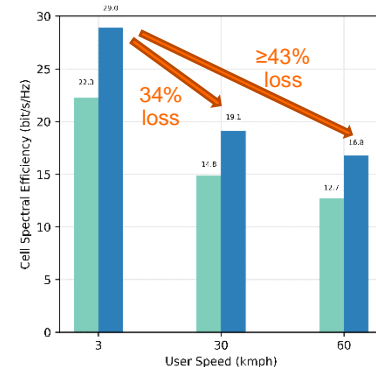
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40msec SRS Periodicity



5msec SRS Periodicity



Significant performance losses ($>43\%$ @ 60kmph) due to channel aging

- Channel prediction methods will help to maintain the massive MIMO gains at higher user speeds
- Overhead due to frequent sounding can be easily compensated by higher cell spectral efficiency

Potential Solution: Predictor Antennas

Without Prediction

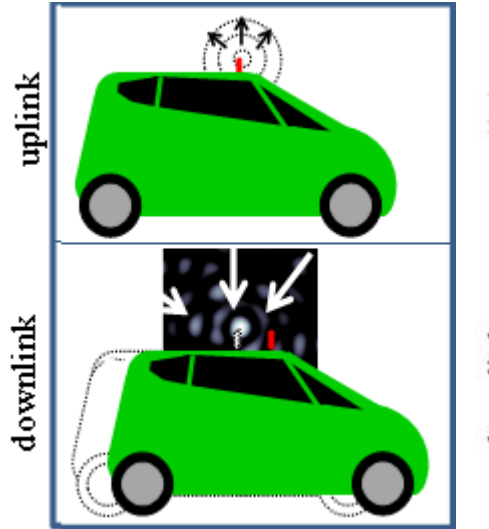
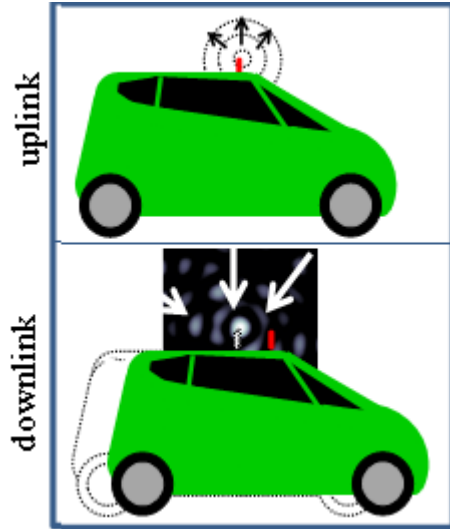


Illustration: Maximum Ratio Transmission (MRT) under heavy multi-path propagation

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With Prediction

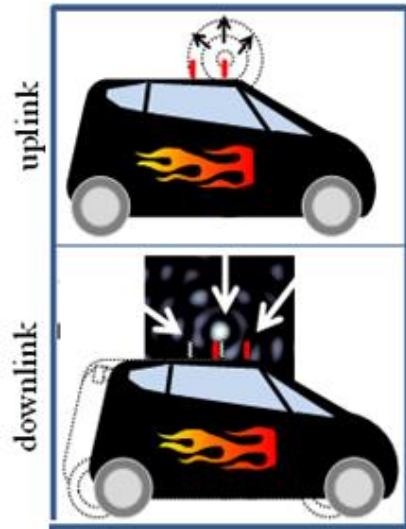


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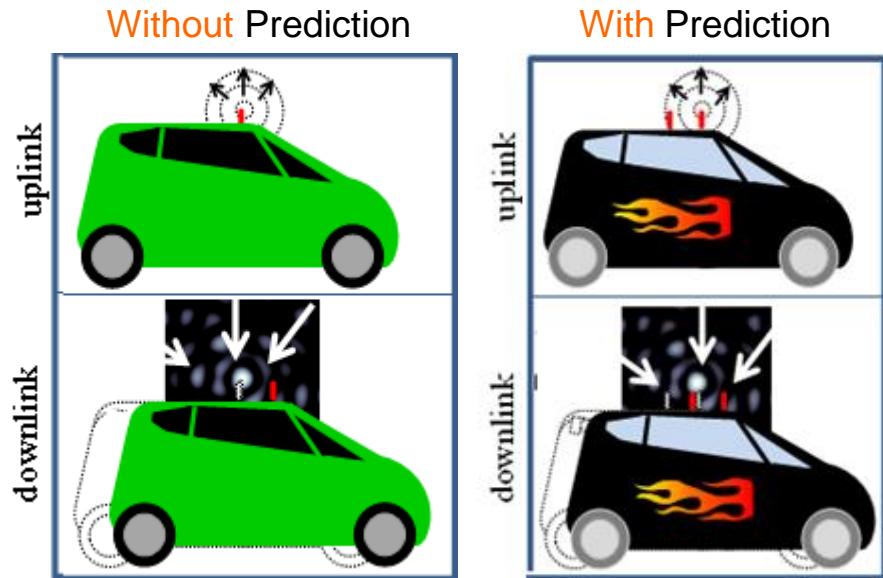


Illustration: Maximum Ratio Transmission (MRT) under heavy multi-path propagation

Maximum speed supported by predictor antenna with

- Antenna distance $d (\geq 0.5\lambda)$
- Delay τ between measurement and BF

$$v \leq \frac{d}{\tau}$$

For $d = 3\lambda$, $\tau = 5\text{msec}$: $v = \frac{d}{\tau} = \frac{0.42}{0.005} = 302 \text{ km/h}$

For $d = 3\lambda$, $\tau = 3\text{msec}$: $v = \frac{d}{\tau} = \frac{0.42}{0.003} = 503 \text{ km/h}$

Requirements:

- Periodicity of UL channel sounding must be small enough to track the channel variations
- Antennas in line and with quasi-equal patterns

Previous Work*: Experimental Verification for SISO Links

Setup in Dresden

- 25-50 km/h user speed,
- OFDM (LTE numerology) at 2.53 GHz,
- Measuring SISO links in sub-urban area,
- Antenna distances $d=\{\lambda/4, \lambda/2, \lambda, 2\lambda, 3\lambda\}$



*) SISO measurement results in [1][2].

15 [1] "Predictor Antennas in Action", Joachim Bjorsell, Mikael Sternad, Michael Grieger, PIMRC 2017.

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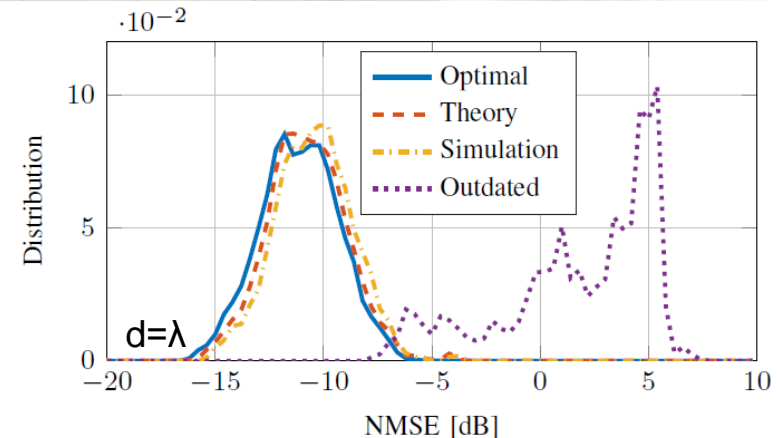
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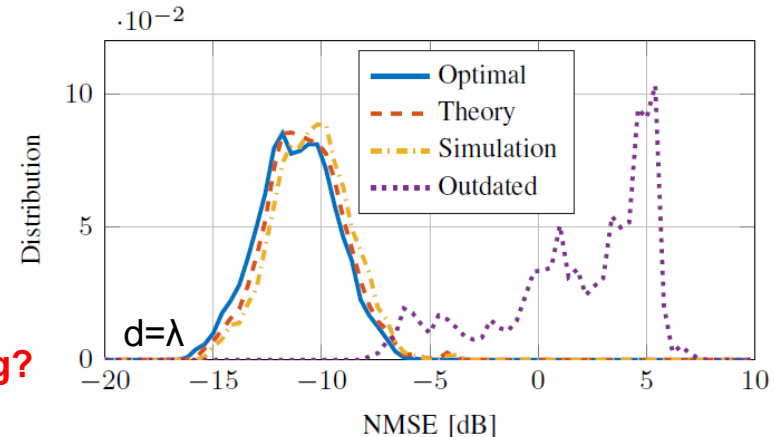


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Remaining question:

How does it combine with massive MIMO beamforming?



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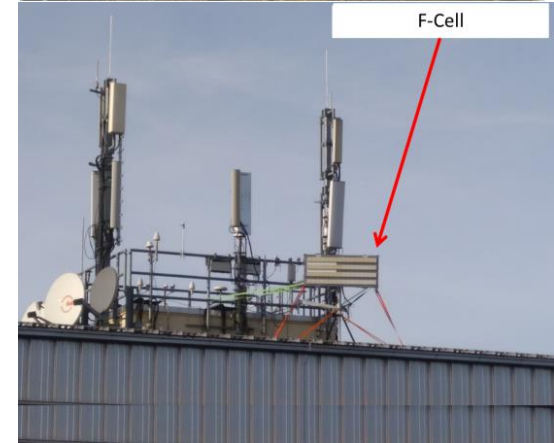
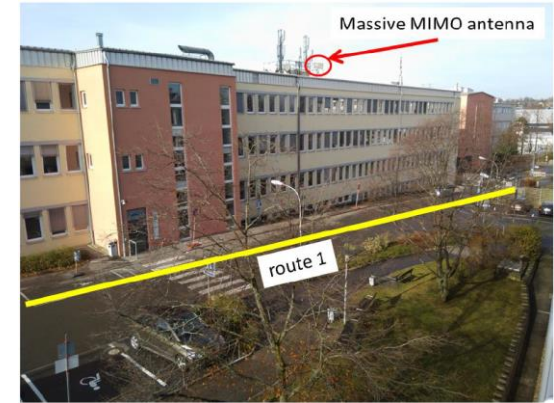
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II. Measurement Setup

Measurement Setup

Network Side Setup:

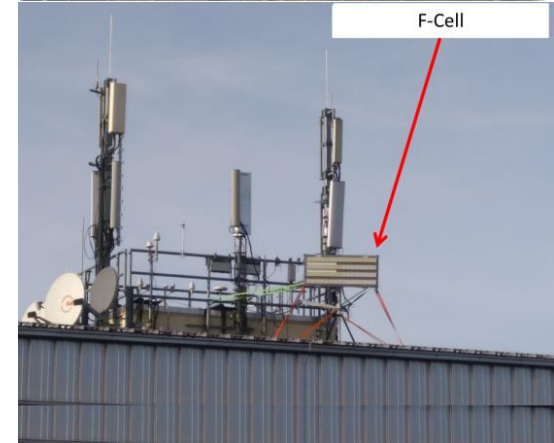
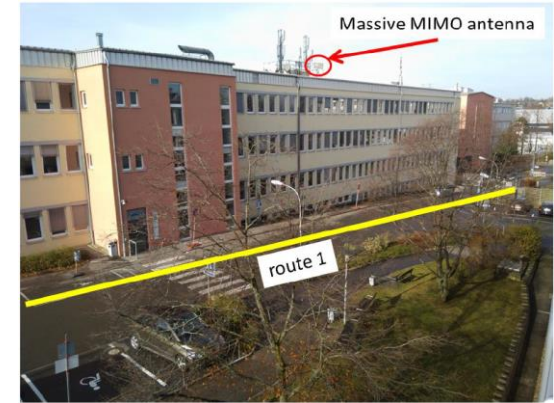
- 64-element antenna array on rooftop of building at a height of 20m
 - Mechanical downtilt of 10 degree,
 - 4 rows with 16 (dual-polarized, but only one polarization direction was used) patch antennas,
 - Horizontal antenna spacing of $\lambda/2$, and a vertical separation of λ ,
 - 2.180 GHz carrier frequency.



Measurement Setup

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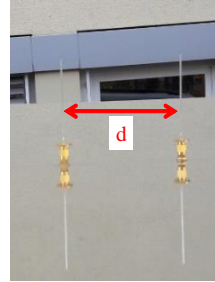
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 - 4 rows with 16 (dual-polarized, but only one polarization direction was used) patch antennas,
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 - 2.180 GHz carrier frequency.
- Pilot signals in downlink
 - Time/frequency-orthogonal pilots (using LTE numerology) for all 64 antenna elements,
 - Pilot burst sent with a periodicity of 0.5msec,
 - For each antenna, 10MHz pilot comb with 180kHz spacing (i.e., 50 subbands over 10MHz).



Measurement Setup

Car Side Setup:

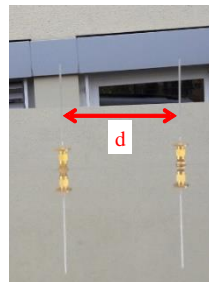
- Frequency synchronization of receiver via Pendulum GPS-12R Portable unit,
- R&S TSMW receiver + R&S IQR hard disk recorder,
- Two receive monopole antennas with distances $d = \{11,15,42\}cm$ mounted on metallic plate, installed upon the roof of the car.



Measurement Setup

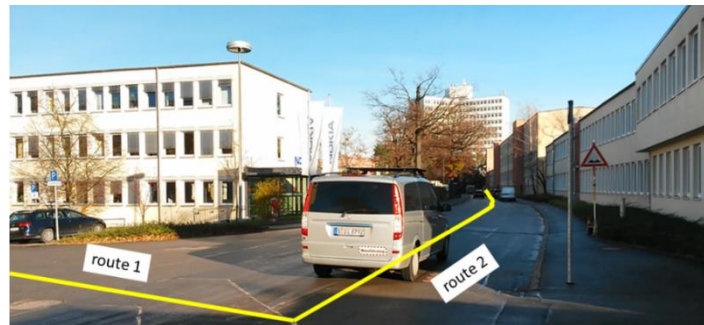
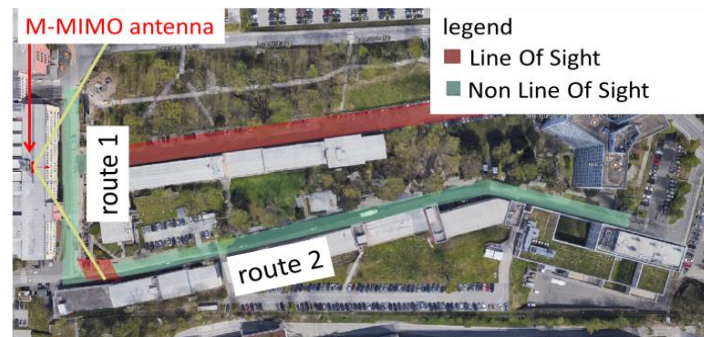
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Measurement Procedure:

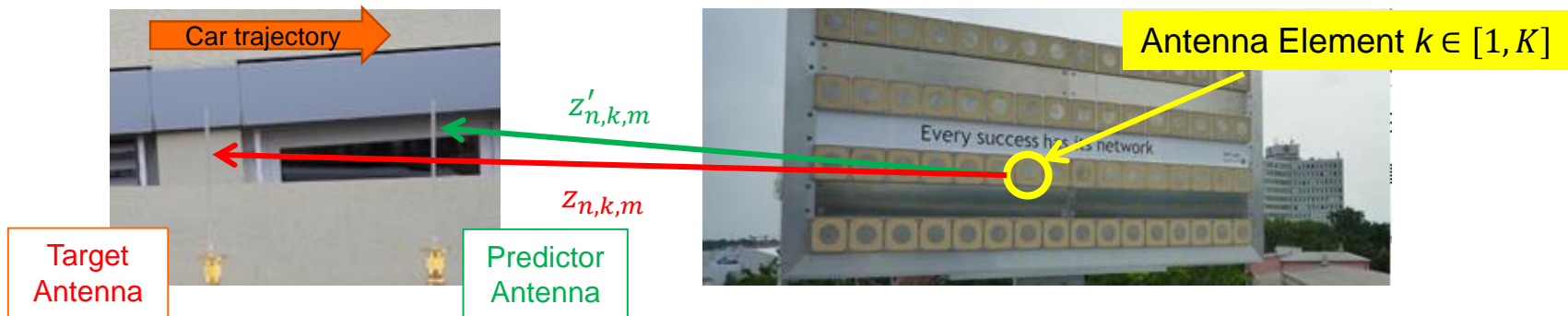
- Two non-line-of-sight routes have been chosen, without any traffic,
- Received pilot signal (at both monopole antennas) is continuously captured along each route over periods of 30s to 40s, with car speeds $v = \{15,25\}kmph$
- Channel estimation (per Tx antenna, subband and pilot burst) is performed offline (achieving NMSEs in the range of -20dB to -30dB without any time/freq.dom. averaging).



III. Performance Evaluation Methodology

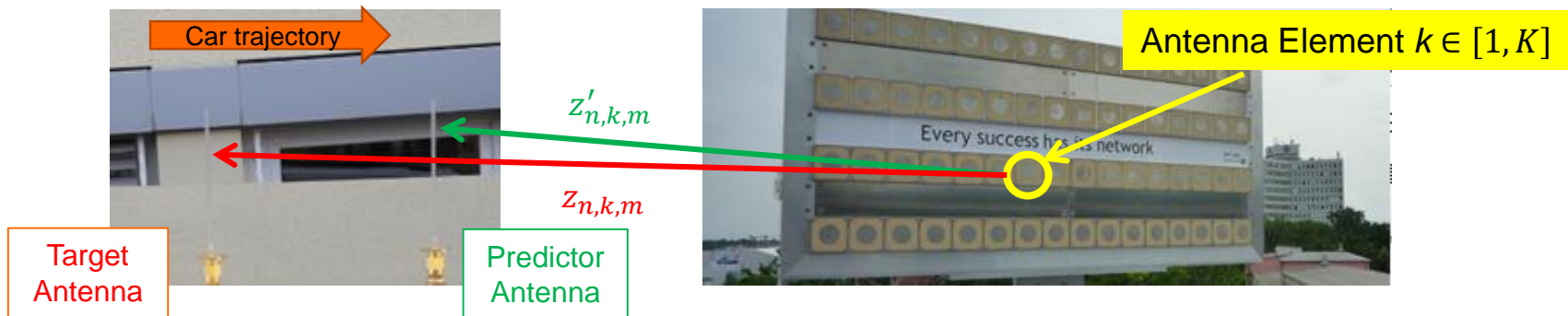
Analyzed Prediction Methods

Measured channel samples at time $n \in [1, N]$, and for frequency index $m \in [1, M]$



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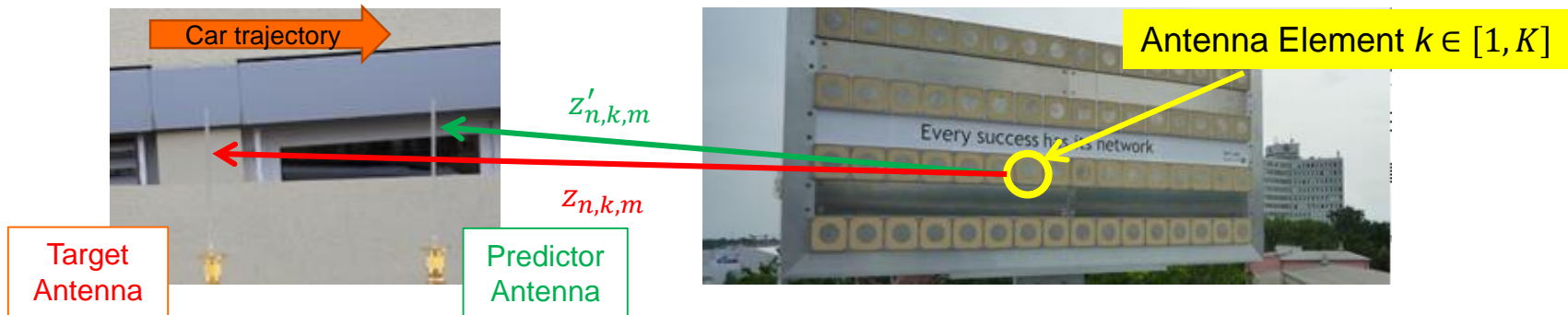


True Channel:

$$h_{n,k,m} = z_{n,k,m}$$

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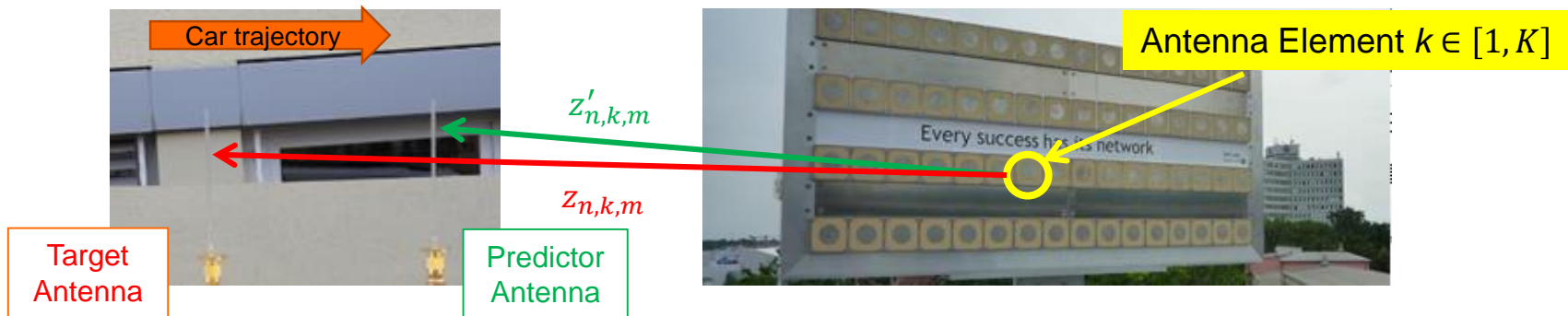
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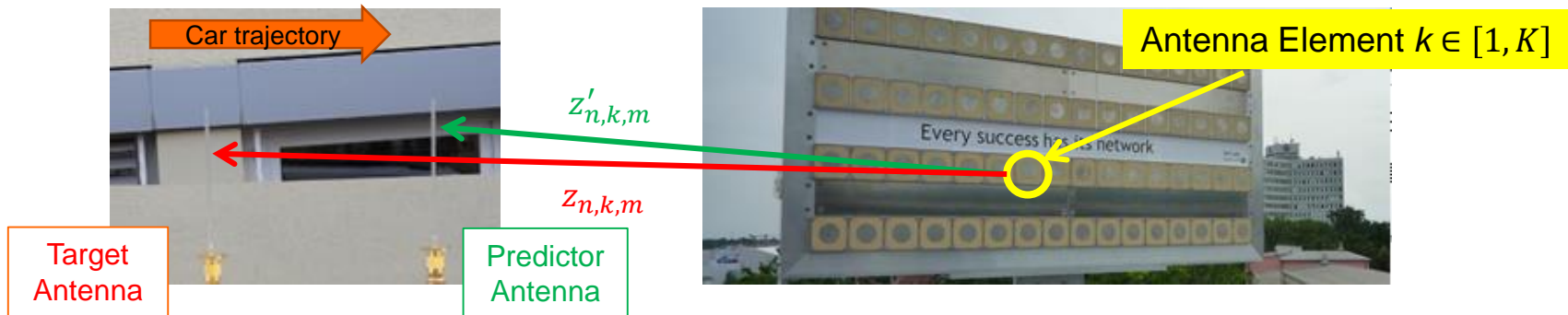
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Outdated Channel:

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Predicted Channel from Predictor Antenna:

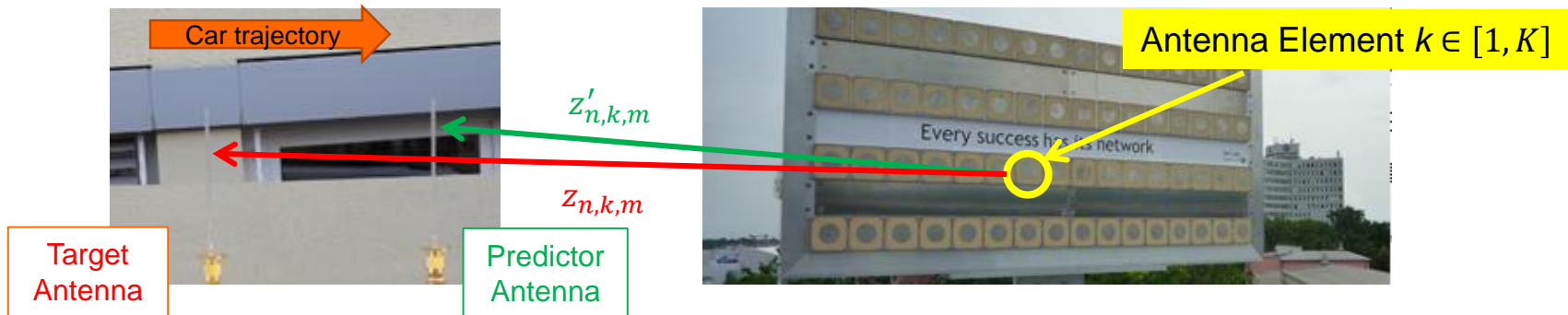
$$h_{n,k,m}^{\text{pred}} = c_{g,k,m} z'_{n-g,k,m}$$

with predictor delay $g = \text{Median}_{k,m} (\arg \max_l |c_{l,k,m}|)$

$$\text{and } c_{l,k,m} = \frac{\sum_{n=N_0}^{N_0+N_1} z_{n,k,m} (z'_{n-l,k,m})^*}{\sqrt{\sum_{n=N_0}^{N_0+N_1} |z_{n,k,m}|^2 \sum_{n=N_0}^{N_0+N_1} |z'_{n-l,k,m}|^2}} \quad (\text{for } N_1 = 1000)$$

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Subsequently, we assume $\tau = g$ (i.e., predictor antenna distance is matched to car speed, $d = \delta$)

Received Power Loss for Maximum Ratio Transmission Beamforming

For timestep n , the **received power** at the data antenna (averaged over all subbands) is

$$r_{\text{ideal}}(n) = \frac{1}{M\alpha_n} \sum_{m=1}^M \left| \sum_{k=1}^K |h_{n,k,m}|^2 \right|^2 \quad \text{with } \alpha_n = \sqrt{\frac{1}{M} \sum_{k=1}^K \sum_{m=1}^M |h_{n,k,m}|^2}$$

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Power loss w.r.t. ideal prediction: $r_{\text{norm}}(n) = \frac{r_{\text{pred}}(n)}{r_{\text{ideal}}(n)}$

Achievable Signal-to-Interference Ratio (SIR) for Zero-Forcing

Zero-forcing for two users with MIMO channel matrix (at time n , subband m) $\mathbf{H}^{(n,m)} \in \mathbb{C}^{2 \times K}$, where

- Predicted channel $h_{n,k,m}^{\text{pred}}$ is used for the first user,
- Circularly-shifted (in freq.dom) channel $h_{n,k,[(m+23)\bmod M]+1}^{\text{pred}}$ is used for a second “imaginary user”.

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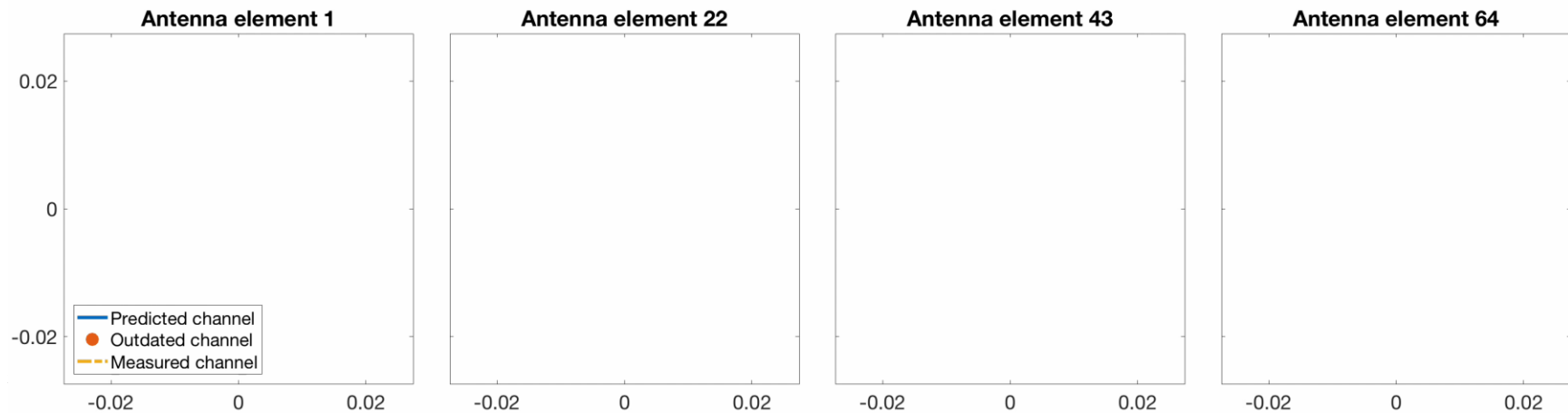
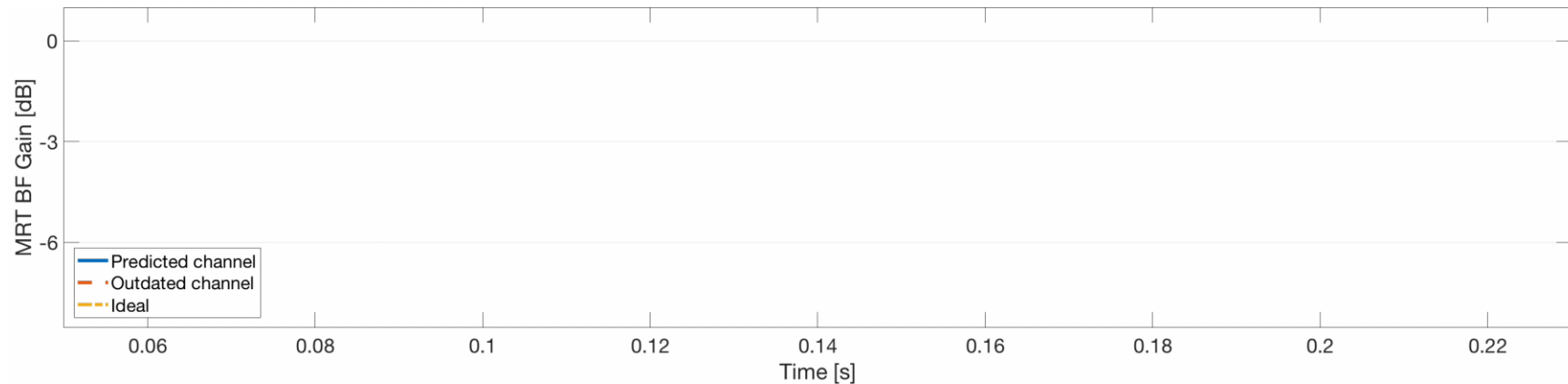
Zero-Forcing precoder: $\mathbf{P}^{(n,m)} = (\mathbf{H}^{(n,m,\text{pred})})^\dagger \left(\mathbf{H}^{(n,m,\text{pred})} (\mathbf{H}^{(n,m,\text{pred})})^\dagger \right)^{-1} \in \mathbb{C}^{K \times 2}$

Effective (beamformed) channel matrix: $\mathbf{G}^{(n,m)} = \mathbf{H}^{(n,m)} \mathbf{P}^{(n,m)} \in \mathbb{C}^{2 \times 2}$

(Average) user SIR for time n , subband m : $\text{SIR}(n, m) = \frac{1}{2} \left(\frac{|\mathbf{G}_{1,1}^{(n,m)}|^2}{|\mathbf{G}_{1,2}^{(n,m)}|^2} + \frac{|\mathbf{G}_{2,2}^{(n,m)}|^2}{|\mathbf{G}_{2,1}^{(n,m)}|^2} \right)$

IV. Results

Illustration for Maximum Ratio Transmission Beamforming



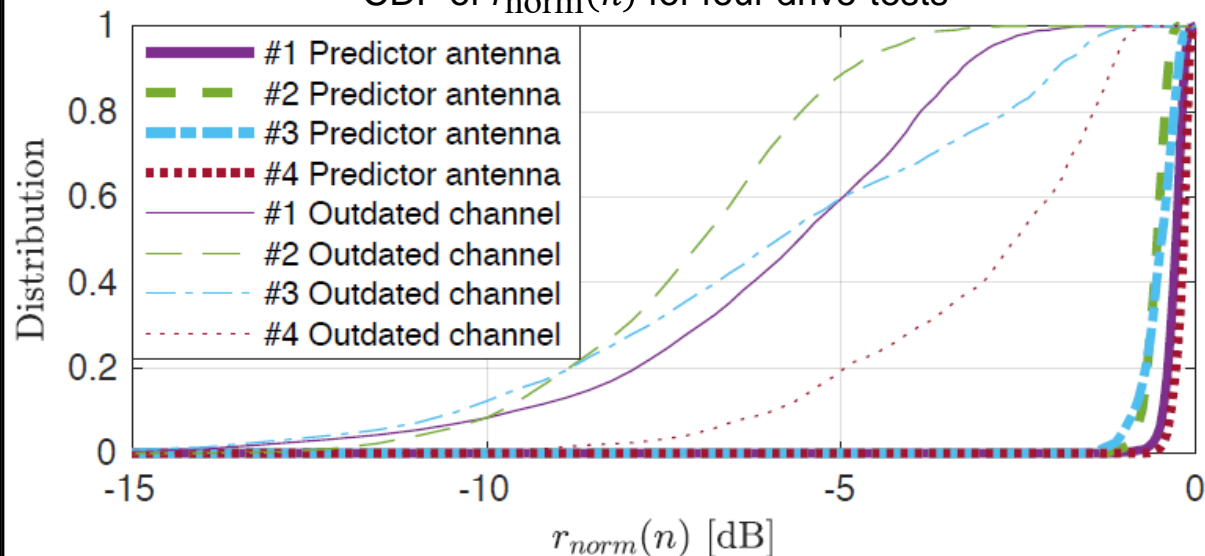
Received Power Loss for Maximum Ratio Transmission

Drive-Tests

N°	Parameters		
	Direction on Route 2	V (km/h)	d (cm)
1	W-E	15	11
2	E-W	25	11
3	W-E	25	42
4	W-E	15	11

11 cm $\sim 0.8\lambda$ and 42 cm $\sim 3\lambda$

CDF of $r_{norm}(n)$ for four drive-tests



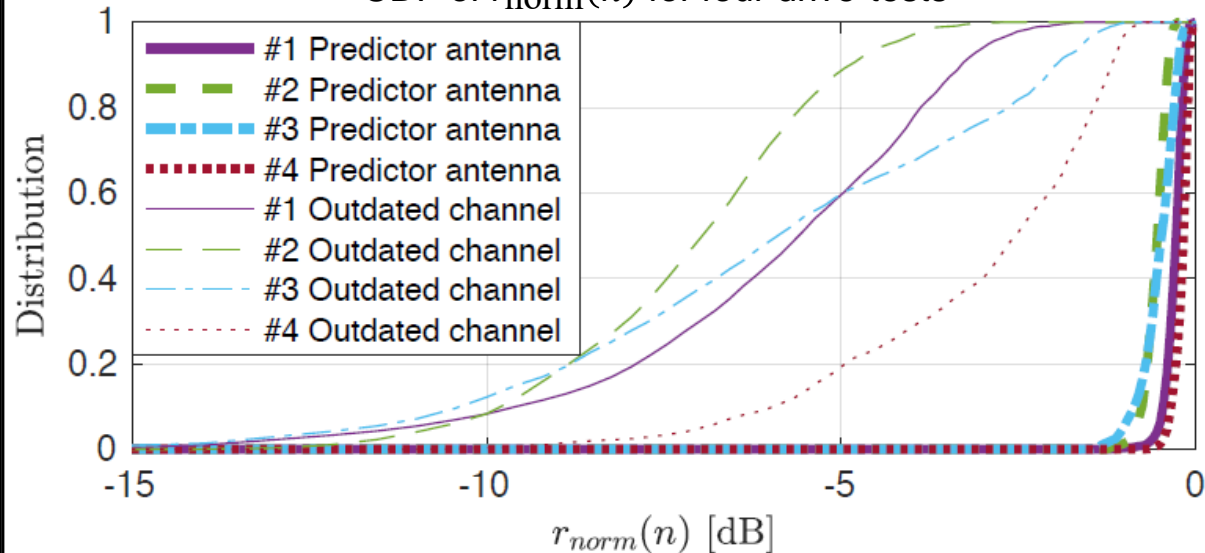
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Predictor antenna reduces the received power losses to less than 1dB!
Prediction horizons of 3λ (and possibly larger) are feasible!

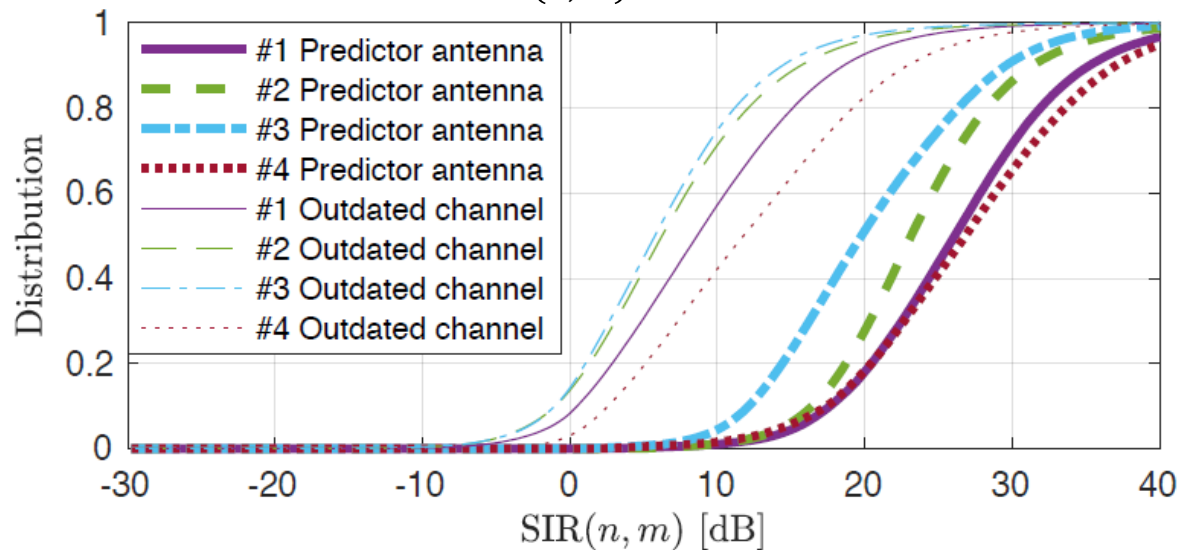
SIR Gain from Predictor Antenna for Two-User Zero-Forcing

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CDF of $SIR(n, m)$ for four drive-tests



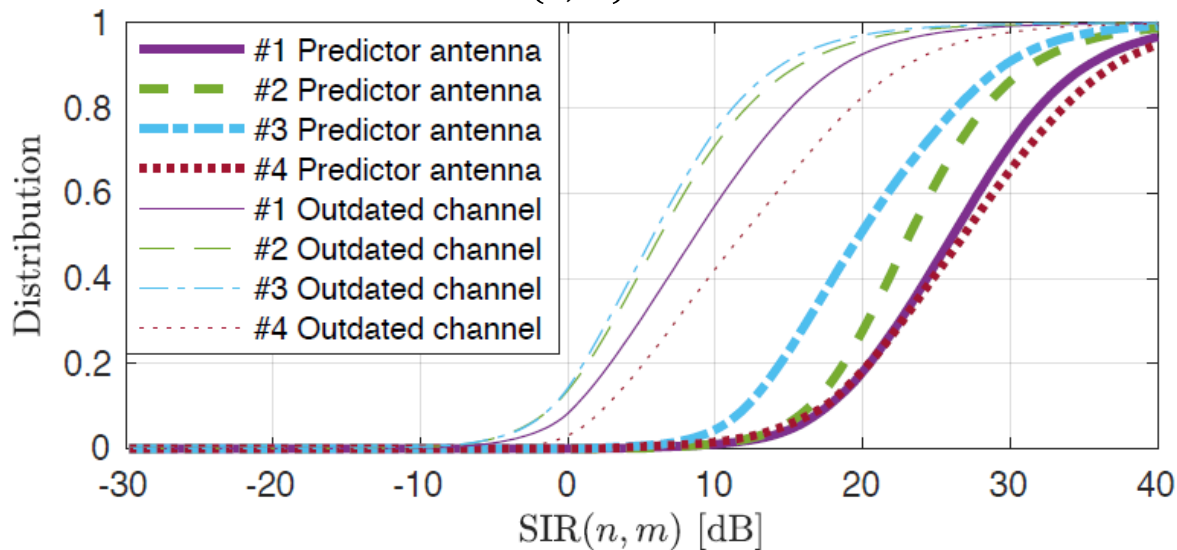
SIR Gain from Predictor Antenna for Two-User Zero-Forcing

Drive-Tests

N°	Parameters		
	Direction on Route 2	V (km/h)	d (cm)
1	W-E	15	11
2	E-W	25	11
3	W-E	25	42
4	W-E	15	11

11 cm $\sim 0.8\lambda$ and 42 cm $\sim 3\lambda$

CDF of $SIR(n, m)$ for four drive-tests



Predictor antenna improves the SIR from typically around 5-15 dB to mostly between 20-30 dB.

Robustness of Our Simple Prediction Method

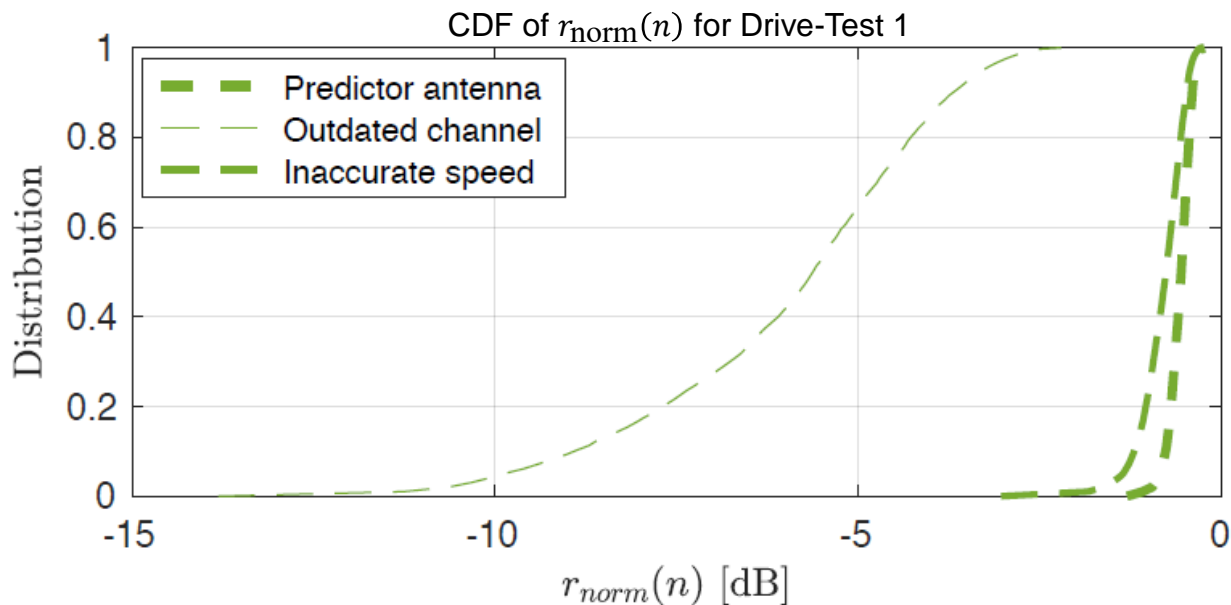
Predicted Channel from **Perturbated/Inaccurate** Predictor Antenna: $h_{n,k,m}^{\text{pred}} = z'_{n-g,k,m}$

with predictor delay $g = \text{Median}_{k,m} (\arg \max_l |c_{l,k,m}|) + \epsilon$ where ϵ is uniformly distributed $[-5,5]$ (i.e., ± 2.5 msec)

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Received power loss due to inaccurate prediction coefficient and delay is remarkably small!

V. Conclusions

V. Conclusions and Next Steps

First & successful experimental measurements for massive MIMO BF and Predictor Antenna:

- A prediction horizon of 3λ has been successfully tested (at 2.180 GHz).
- This enables the application of (MRT) beamforming for high velocities.
- Limited accuracy with the predictor is good enough for massive MIMO MRT.

Latency τ	Support Car Speed $v = \frac{d}{\tau}$
3 ms	302 km/h
5 ms	503 km/h

Next steps:

1. Investigating prediction methods for the general case of $\tau \neq g$.
2. Running and evaluating a real-time prediction algorithm based on the Predictor Antenna concept, assuming a realistic time-frame structures in TDD systems (SRS periodicity).
3. Evaluate the hardware, software and system design factors that affect the performance of a predictor antenna system.

Thank You!



Any Questions?

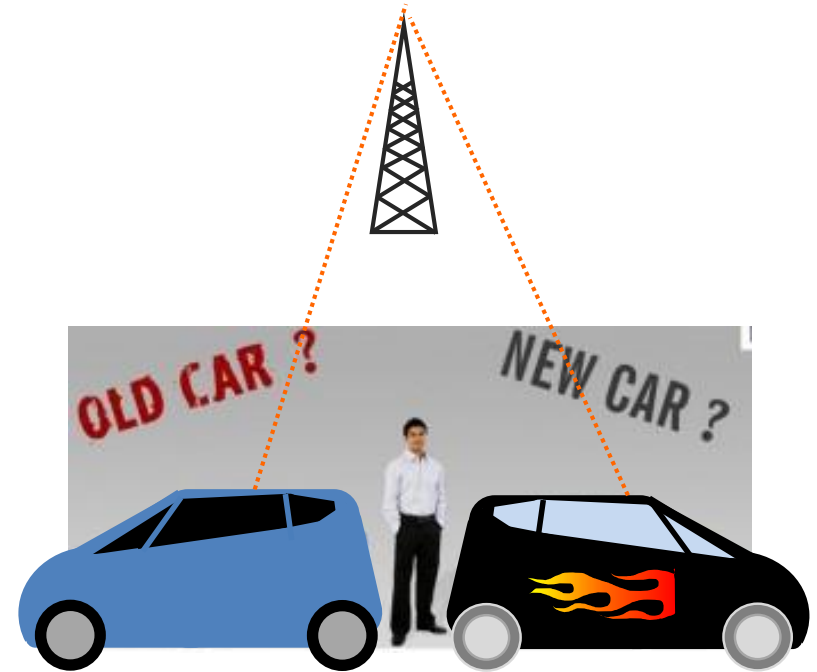
Guenter Kaltbeitzel¹, Prof. Mikael Sternad², Dinh-Thuy Phan-Huy³, Joachim Bjorsell², Stefan Wesemann¹

45 ¹Nokia Bell Labs, ²Uppsala University, ³Orange Labs

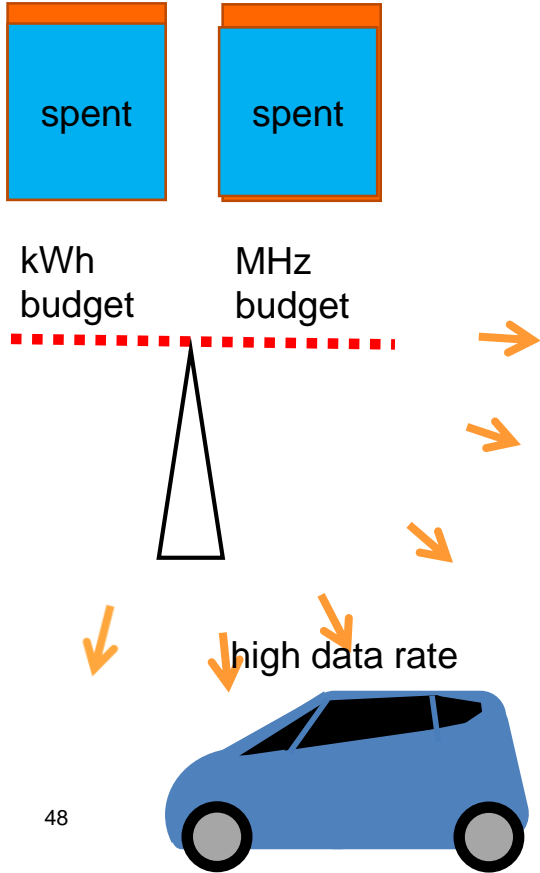
Annex

I. Introduction

- Do we really need to change anything?
- How many antennas do we need to put on connected cars?



I. Introduction



Not a problem for Operators today,
due to low load of connected cars

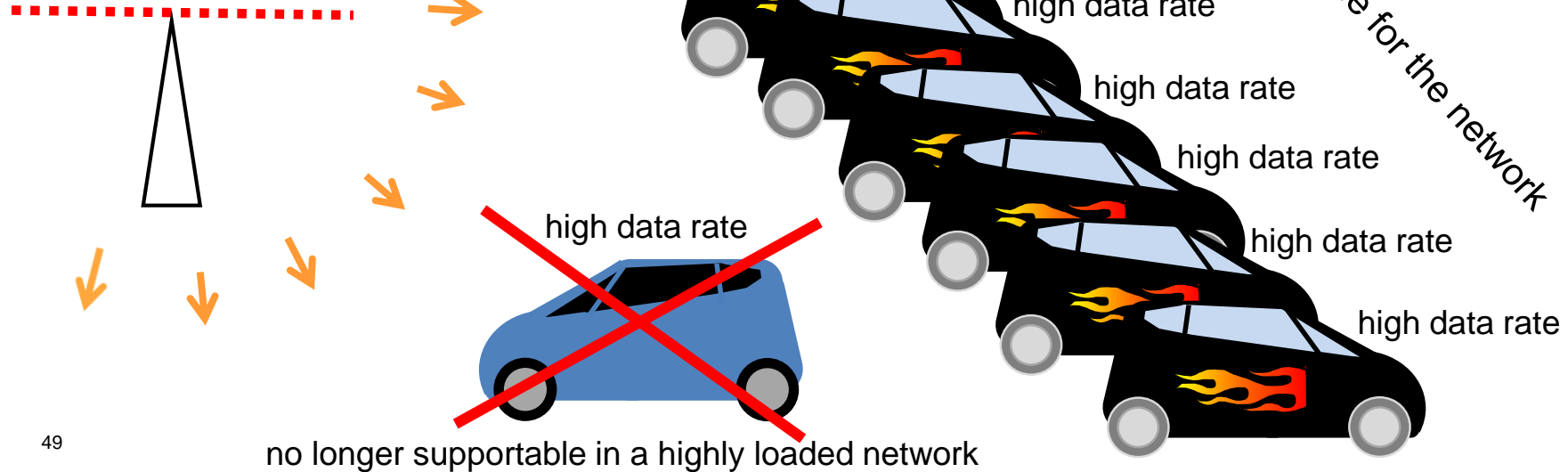
supportable for the network

I. Introduction

A problem >2020 for Operators,
due to high load of connected cars

spent	spent
spent	spent
spent	spent
spent	spent
spent	spent
spent	spent

kWh budget
MHz budget



Prediction is useful whatever the ideal received BF gain

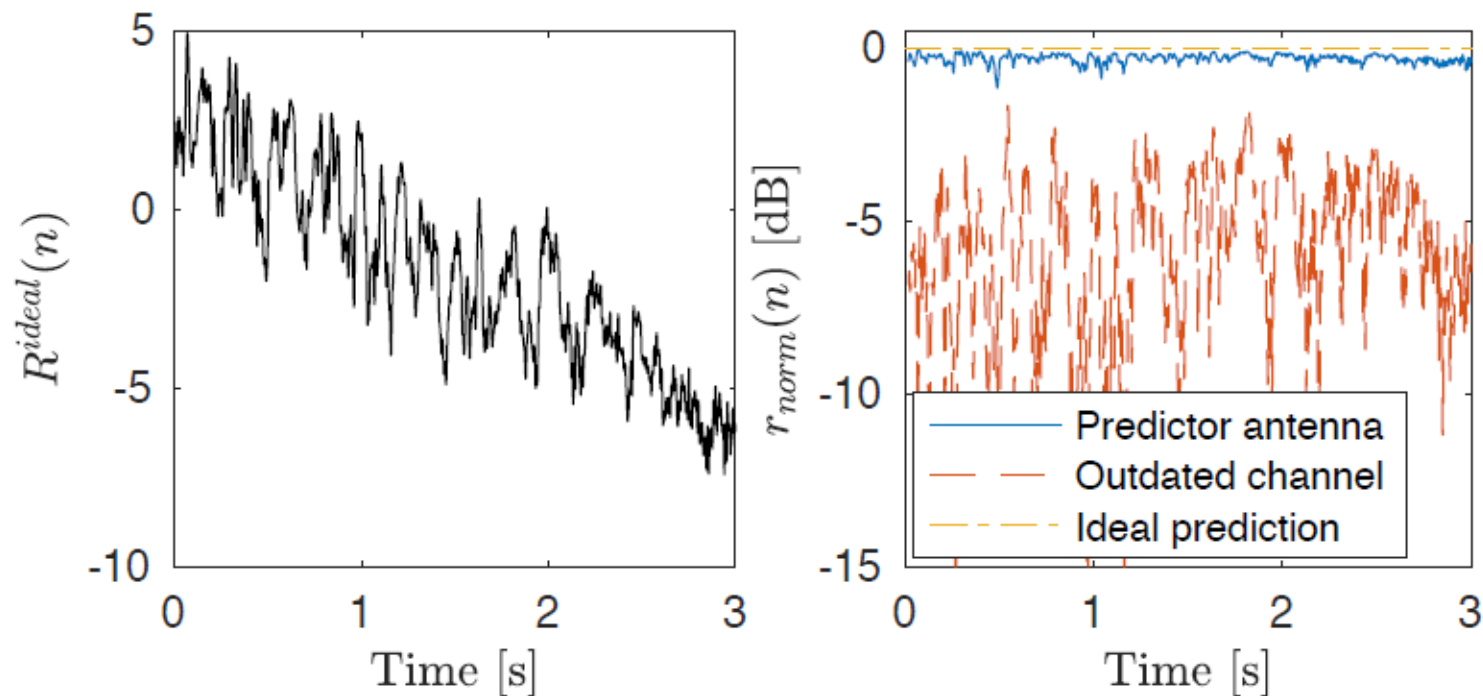


Fig. 8. Time evolution of received ideal beamformed power by (17) (left) and the normalized received power by (10) (right), in Drive-Test 1.

Line-Of-Sight vs Non Line Of Sight

Probably LOS: high received power no huge gain due to Prediction

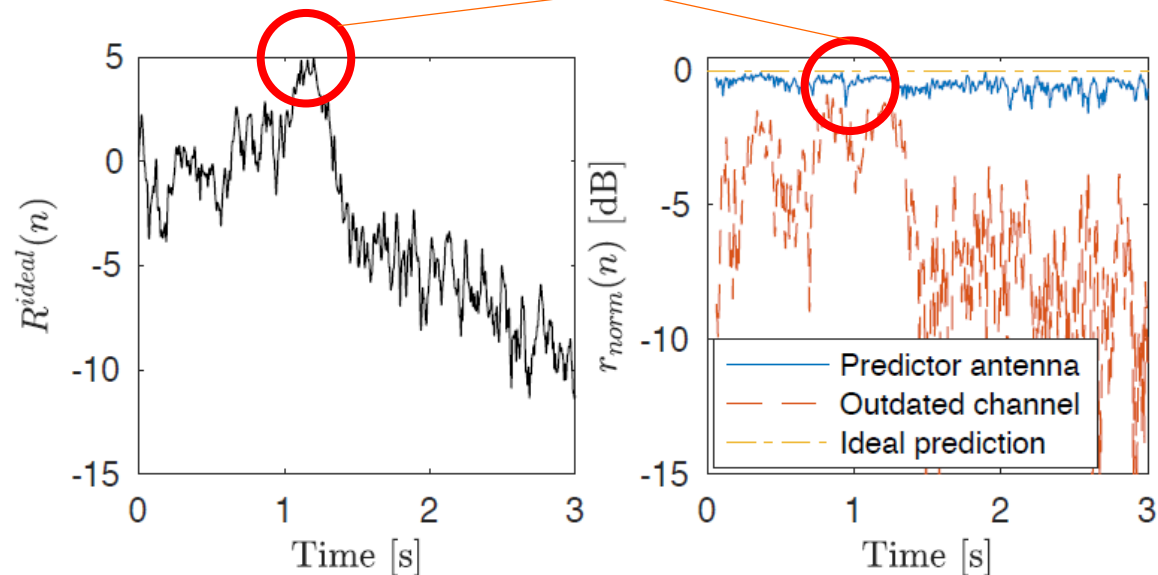


Fig. 9. Time evolution of received ideal beamformed power by (17) (left) and the normalized received power by (10) (right), in Drive-Test 3.

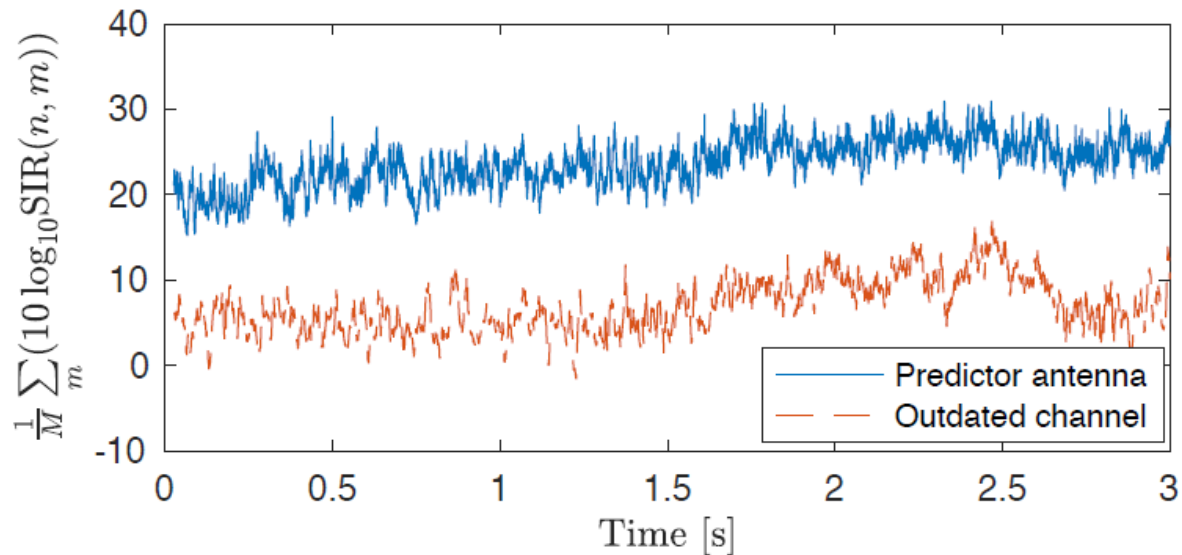
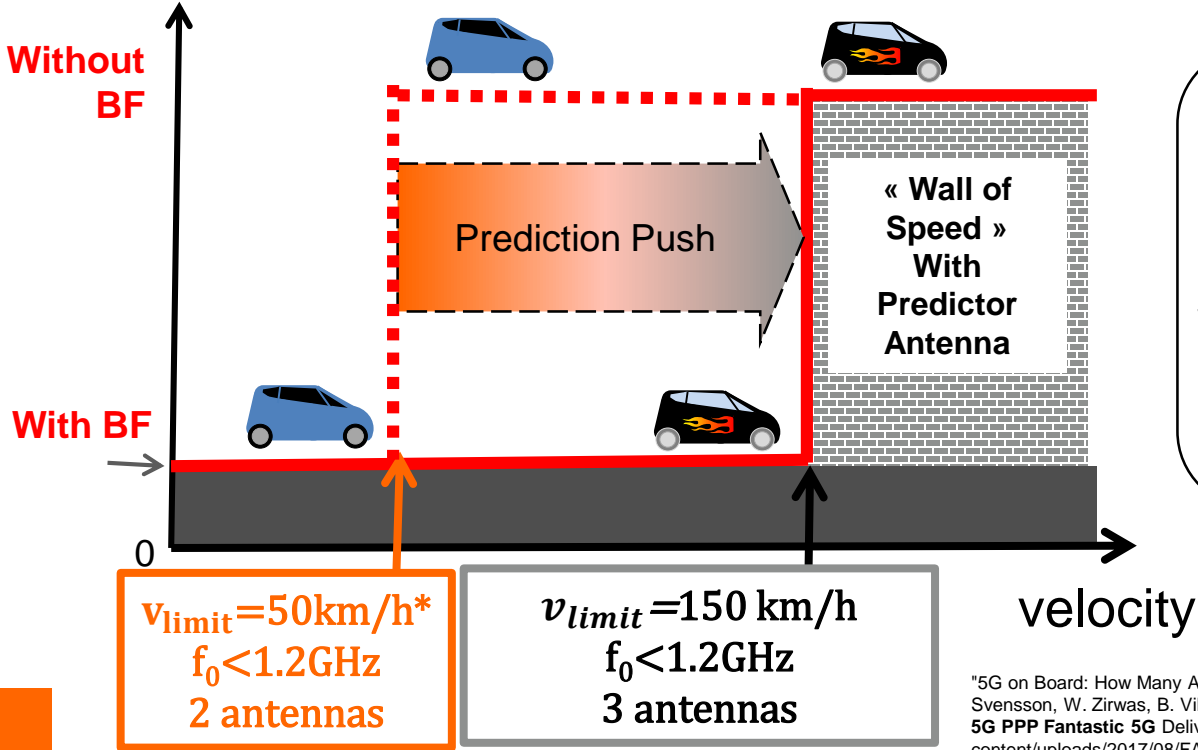


Fig. 11. The residual SIR, averaged for the two users and averaged over all subcarriers, along Drive 2, when applying zero forcing transmit beamforming using channels estimates from predictor antennas and outdated channel estimates.

Previous simulation studies on Wall of Speed for M-MIMO BF

Wall of speed for 256x1 MRT Beamforming, based on simulations

cost in power



$$v_{wall}(f) = \frac{C_{wall}}{f}$$

Values of C_{wall} determined by simulation in [1][2]

"5G on Board: How Many Antennas Do We Need on Connected Cars?", D.-T. Phan-Huy, M. Sternad, T. Svensson, W. Zirwas, B. Villeforceix, F. Karim, S.-E. El-Ayoubi, **IEEE Globecom 2016**.
 5G PPP Fantastic 5G Deliverable D2.3 (http://fantastic5g.com/wp-content/uploads/2017/08/FANTASTIC-5G_D2.3_final.pdf)